Math. 350-01
Summer, 2017
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## Fourth Exam

Monday, July 24, 2017, 8:00-9:00AM
This exam is closed book, but you may use calculators. Make sure your name is on all pages. Show all work, and show it in a logical and organized manner.

- (Refer to Table 1 to do this problem.) Use Laplace transforms to find the solution to

$$
y^{\prime \prime}+y=\sin (2 t)-u_{2 \pi}(t) \sin (2(t-2 \pi)), \quad y(0)=0, \quad y^{\prime}(0)=1 .
$$

Table 1: Table of Laplace Transforms
6.2 Solution of Initial Value Problems

TABLE 6.2.1 Elementary Laplace Transforms

|  | $f(t)=\mathcal{L}^{-1}\{F(s)\}$ | $F(s)=\mathcal{L}\{f(t)\}$ | Notes |
| :---: | :---: | :---: | :---: |
| 1. 1 | $\frac{1}{s}$, | $s>0$ | Sec. 6.1; Ex. 4 |

2. $e^{a t}$
3. $t^{n}, n=$ positive integer
4. $t^{p}, \quad p>-1$
$\frac{\Gamma(p+1)}{s^{p+1}}, \quad s>0$
Sec. 6.1;Ex. 5
$\frac{n!}{s^{n+1}}, \quad s>0$
Sec. 6.1; Prob. 27
$\frac{a}{s^{2}+a^{2}}, \quad s>0$
Sec. 6.1; Prob. 27
5. $\sin a t$
6. $\cos a t$
7. $\sinh a t$
8. $\cosh a t$
$\frac{s}{s^{2}-a^{2}}, \quad s>|a|$
9. $e^{a t} \sin b t$
$\frac{b}{(s-a)^{2}+b^{2}}, \quad s>a$
$\frac{s-a}{(s-a)^{2}+b^{2}}, \quad s>a$
10. $t^{n} e^{a t}, n=$ positive integer
$\frac{n!}{(s-a)^{n+1}}, \quad s>a$
11. $u_{c}(t)$
$\frac{e^{-c s}}{s}, \quad s>0$
$e^{-c s} F(s)$
12. $e^{c t} f(t)$
13. $f(c t)$
14. $\int_{0}^{t} f(t-\tau) g(\tau) d \tau$
15. $\delta(t-c)$
16. $f^{(n)}(t)$
17. $(-t)^{n} f(t)$
$F^{(n)}(s)$

Sec. 6.1;Ex. 6

Sec. 6.1; Prob. 6

Sec. 6.1; Prob. 8

Sec. 6.1; Prob. 7

Sec. 6.1; Prob. 13

Sec. 6.1; Prob. 14

Sec. 6.1; Prob. 18

Sec. 6.3

Sec. 6.3

Sec. 6.3

Sec. 6.3; Prob. 19

Sec. 6.6

Sec. 6.5

Sec. 6.2

Sec. 6.2; Prob. 28

