

① $f'(x) = x^2 - 3x + 2 = 0$ where $(x-1)(x-2) = 0$, that is, at $x=1$ and $x=2$.

$$f''(x) = 2x - 3.$$

$f''(1) = 2 - 3 = -1 < 0$, so $x=1$ corresponds to a local maximum.

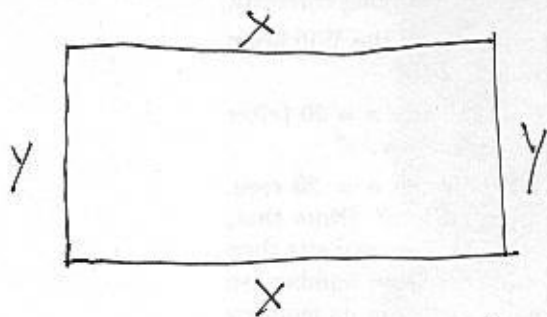
$f''(2) = 4 - 3 = 1 > 0$, so $x=2$ corresponds to a local minimum.

② We list the possible candidates:

Thus, the global maximum is 1.5, and it occurs at the endpoint $x=3$, while the global minimum is -28.5, and it occurs at the endpoint $x=-3$.

x	$f(x)$
-3	-28.5 ← min
3	1.5 ← max
1	.8 $\bar{3}$
2	.6

③



We want to minimize
 $C = 5x + 10x + 3y + 3y$
 $= 15x + 6y$
 subject to $xy = 100,000$.

This gives $y = 100,000/x$, so

$$C(x) = 15x + \frac{600,000}{x} \quad C'(x) = 15 - \frac{600,000}{x^2} = 0$$

$$\Rightarrow x^2 = 40,000 \Rightarrow \boxed{x = 200 \text{ ft}, y = 500 \text{ ft.}}$$

This is apparently a ~~maximum~~ ^{minimum} cost, since $C''(x) = \frac{300,000}{x^3} > 0$.

The minimum cost is thus

$$\$ (15(200) + 6(500)) = \$6,000.$$

$$(4) I = V/R. \quad \frac{dI}{dt} = \frac{dI}{dR} \frac{dR}{dt} = -\frac{V}{R^2} \frac{dR}{dt}.$$

$$\text{Thus, } \frac{dI}{dt} = \frac{-12}{2^2} (.5) = \boxed{-1.5 \text{ amperes per second}}.$$

$$(5) (a) \lim_{x \rightarrow 0} \frac{\sin^2 x}{x^2} = \lim_{x \rightarrow 0} \frac{2 \sin x \cos x}{2x} = \lim_{x \rightarrow 0} \frac{\sin(2x)}{2x}$$
$$= \lim_{x \rightarrow 0} \frac{2 \cos 2x}{2} = \boxed{1}.$$

$$(b) \lim_{x \rightarrow \infty} \frac{\ln(x)}{x} = \lim_{x \rightarrow \infty} \frac{1}{x} = 0.$$

$$(c) \lim_{x \rightarrow \infty} \frac{x^2 + 3x + 2}{x^2 \ln x} = \lim_{x \rightarrow \infty} \frac{2x + 3}{2x \ln x + x}$$
$$= \lim_{x \rightarrow \infty} \frac{2}{2 \ln x + 2 + 1} = \boxed{0}.$$